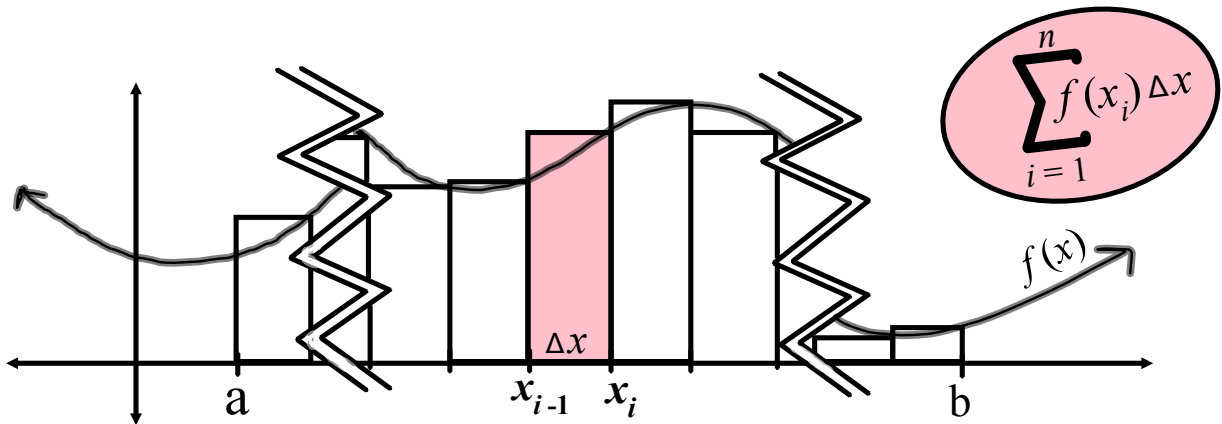


# Calculus AB

4-2 (Day 2)  
Riemann Sums

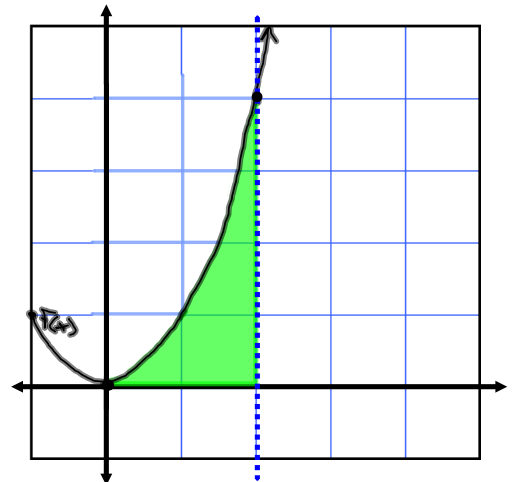
The following is an approximation for area beneath a curve using Right Hand estimation. The formula used to find such an area is called a **Riemann Sum**.



- 1) What does  $x_i$  equal in terms of  $a$ ?  $x_i =$  \_\_\_\_\_
- 2) What is  $a$  in terms of  $x$ ?  $a =$  \_\_\_\_\_
- 3) What does  $b$  equal in terms of  $a$ ?  $b =$  \_\_\_\_\_
- 4) To get a better estimate of the area, what must be true of  $n$ ? \_\_\_\_\_
- 5) As  $n$  increases, which value must decrease? \_\_\_\_\_
- 6) To get an exact area, what must we do? \_\_\_\_\_
- 7) As the limit as  $n \rightarrow \infty$ ,  $\Delta x \rightarrow$  \_\_\_\_\_

## Definite Integral -

Find the area bounded by the  $x$ -axis and  $f(x) = x^2$  between 0 and 2.



Compare all.

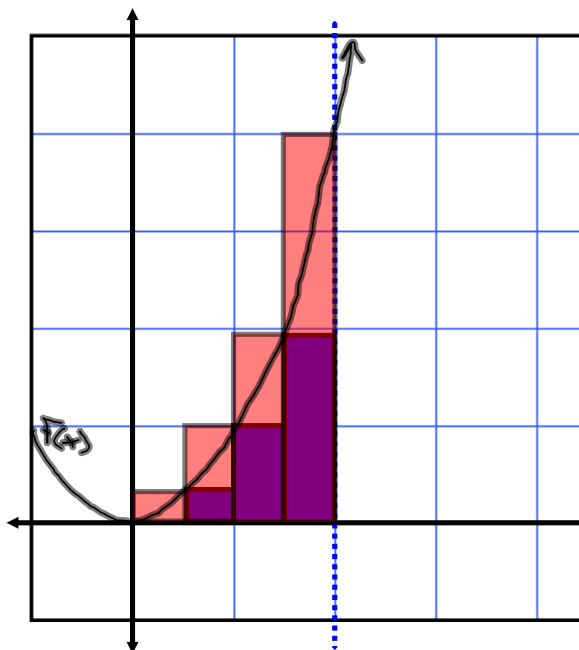
Right Hand estimate -

Left Hand estimate -

Midpoint estimate -

Average of Left and Right -

Actual area using integrals -



Use the limit process to find the area of the region between the graph of the function and the  $x$ -axis over the indicated interval. (pg 269)

58)  $y = 3x - 2$        $[2,5]$

70)  $f(y) = 4y - y^2$        $[1,2]$

Assignment:  
Pg. 269  
57 - 71 odd